

Economic Scenario Generators

A regulator's perspective

Falk Tschirschnitz, FINMA
Bahnhofskolloquium

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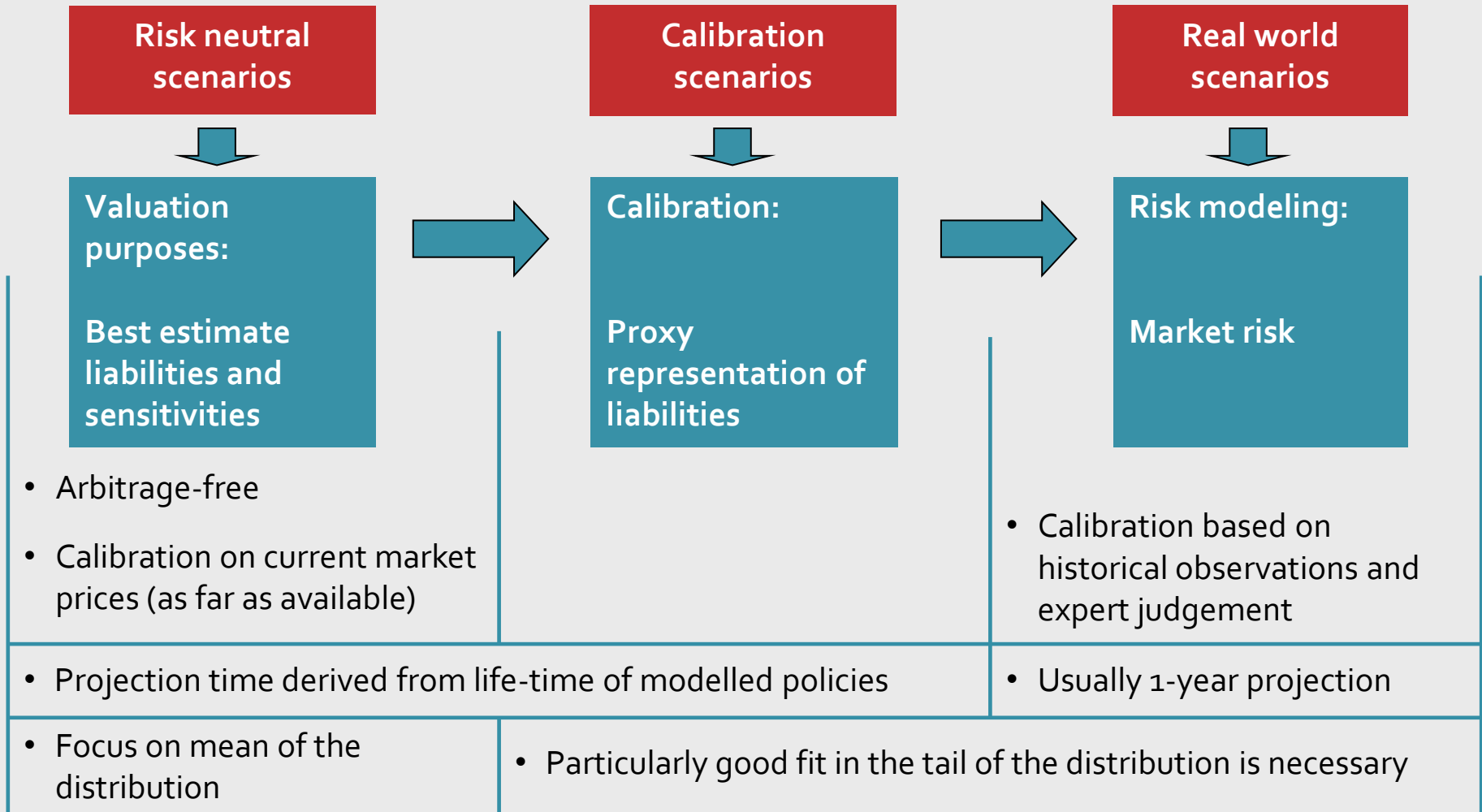
FINMA has observed:

- Calibrating the interest rate model of choice has become increasingly difficult:
 - High implied volatilities, undulating surface
 - Extremely low nominal interest rates, even negative
- Documentation of the ESG as part of the internal model is usually very limited
 - Choice of particular model is not explained
 - Limitations of the chosen model are not discussed

→ The model risk is considerable.

- Why do we need Economic Scenario Generators (ESGs) ?
- What are the key properties an ESG should fulfil?
- How can you assess the adequacy of your model choice?

Different uses ask for different types of scenario sets



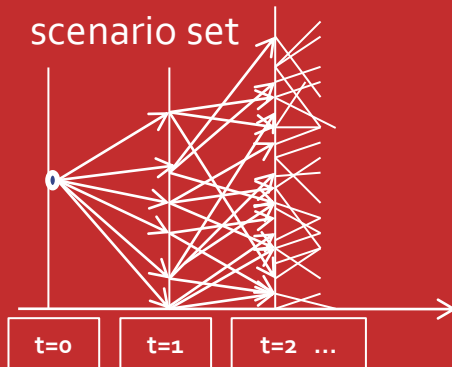
are at the core of stochastic modelling

- An ESG produces forward-looking scenarios for a specified set of risk factors, e.g.:
 - Interest rate term-structures
 - Inflation
 - Index returns, e.g. for equity, real estate, hedge funds, private equity
 - Exchange rates
- *Assumption:*
The possible behaviour of risk factors (and their interaction) can be described sufficiently well by certain stochastic models
- Choice of the stochastic model and a set of parameters determines the range of the scenarios produced by ESG

Most life insurers require complex stochastic models finma for valuation of their liabilities at reference day

Input data

- Policy data
- Statutory balance sheet ($t=0$)
- ...
- Risk-neutral economic scenario set



Best estimate liabilities

Cash flow model

Statutory P&L /
Balance sheet

Dynamic management actions
e.g. bonus crediting

Fund-based policyholder
benefits and fees

Dynamic policyholder actions
e.g. lapses

Monte Carlo simulation is currently the only feasible method to value complex (life) liabilities



- Idea behind Monte Carlo method:
 - Generate sample paths for set of risk factors over the modelling period.
 - Calculate the (discounted) cash flows of the sample paths.
 - Aggregate the results.
- **Key idea & assumptions for market consistent valuation:**
 - We start in a risk-neutral setting by calibrating the ESG to market prices of options and derivatives from deep and liquid markets. (This setting is free of arbitrage.)
 - Best estimate for the liabilities is calculated as expectation.
 - Property of arbitrage-freeness is not affected.
 - Economically coherent.

Valuation of life liabilities: Survey of Swiss companies

- All companies with materially sized business allowing for policyholder participation are expected to model stochastically
- Number of risk factors varies
 - between 3 (nominal interest rate / inflation / equity index)
 - and ~15 (multi-economy / various indices / credit spread)
- Two providers dominate the market, hence the choice of models limited
 - for nominal interest rate: Hull-White / 2Factor-Black-Karasinski / LMM(+)

The choice of the ESG poses some key challenges

- Choice of modelled risk factors
 - Choice of ESG-provider

 - Choice of complexity of the model
 - Trade-off between simplicity and (perceived) accuracy
 - Choice of calibration targets
 - Limited availability / reliability of market prices
 - Limited relevance of historical data for future predictions
- Actuarial judgement essential that cannot be fully externalised
- All decisions need to be documented

- Arbitrage free (for valuation purposes)
- Technically, fit for purpose
 - Theoretical basis
 - Data used is accurate, complete and appropriate
 - Robust calibration process

- **Adequate :**

“No more complex than necessary,
given the specific purpose and usage (e.g. product portfolio)”

(Parsimonious principle)

The complexity of the ESG should be adequate to the complexity of the valuation model

“Too simple”

Big calibration error

Optionality in the liabilities not captured

Model only working for a certain range of interest rates / volatilities

“Just right”

Extremely difficult calibration

“pseudo-accuracy”

ESG as black box

“Too complex”

Required properties for IR-models for risk-neutral valuation (1/5)

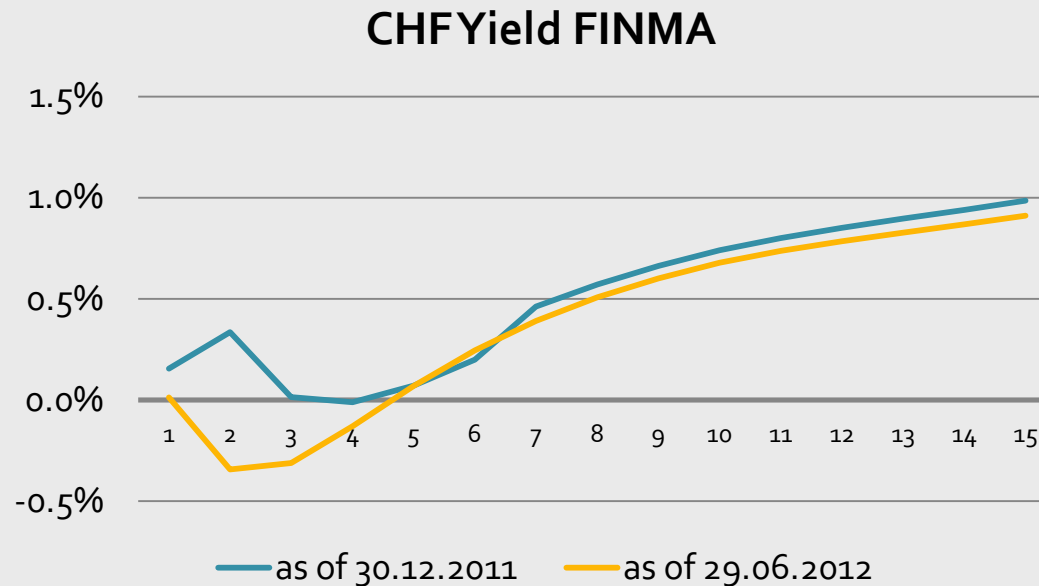
- Arbitrage free

Relevant criteria:

- Martingale test:
all asset classes achieve the same average return
- Leakage test:
starting market value of assets (MVA) should be equal to the present value of all future cash flows plus the present value of the residual MVA

Required properties for IR-models for risk-neutral valuation (2/5)

- Can be calibrated to initial term structure



Relevant criteria:

Initial bond prices are perfectly matched.

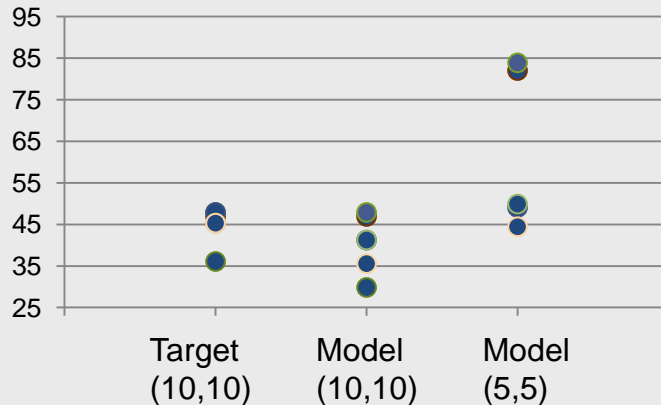
Required properties for IR-models for risk-neutral valuation (3/5)

- Can be calibrated to initial derivative prices

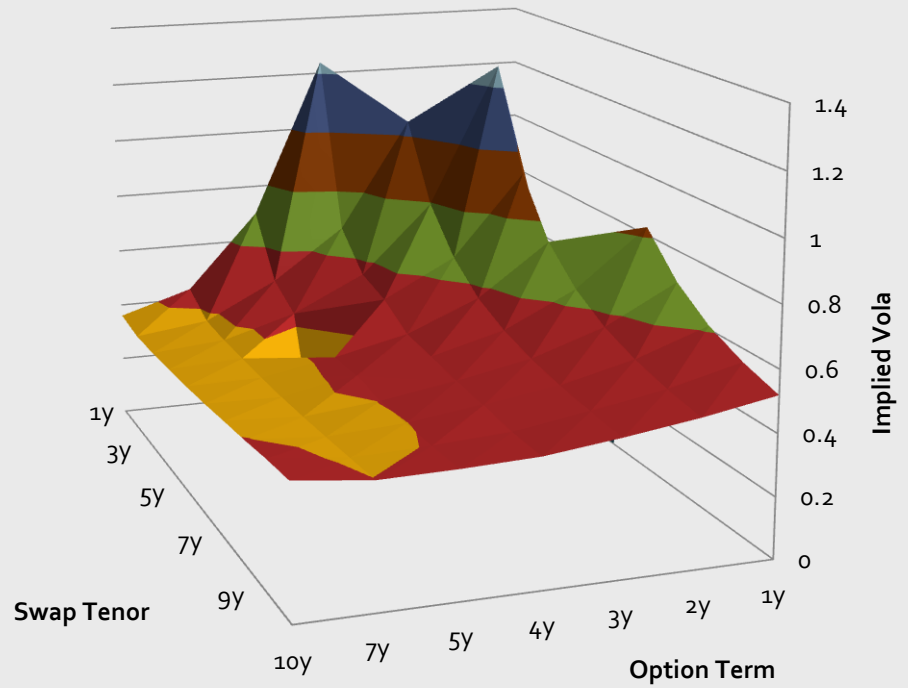
Relevant criteria:

- Clear acceptance criteria
- Robust calibration process

Imp Vol in % -- Assumptions used for SST 2012



CHF implied swaption vol
as of 30.06.12
Source: Bloomberg



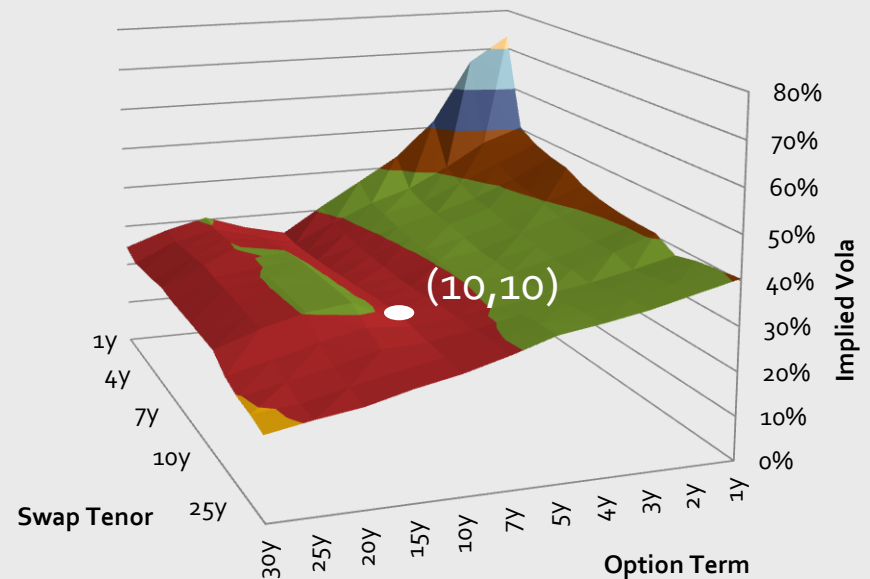
Required properties for IR-models for risk-neutral valuation (3/5)

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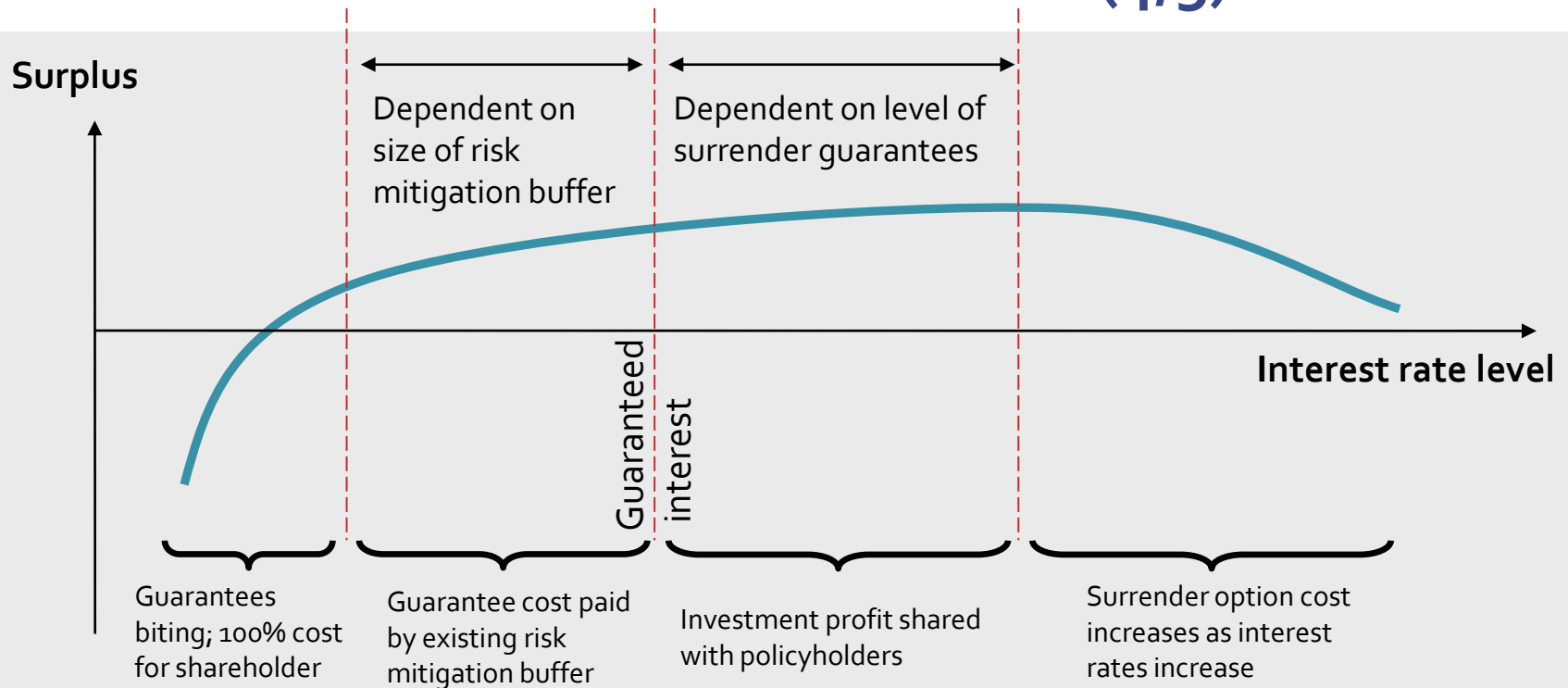
Relevant criteria:

- Clear acceptance criteria
- Robust calibration process
- Well chosen calibration targets

EUR implied swaption vol
as of 30.06.12
Source: Bloomberg



Required properties for IR-models for risk-neutral valuation (4/5)



- Produces sufficiently rich set of yield curve movements

Relevant criteria:

TVOG not underestimated by choice of interest rate model
(e.g. path-dependencies likely to be mispriced by 1-factor model)

Required properties for IR-models for risk-neutral valuation (5/5)

- Theoretically sound, numerically stable
- Valuation model and ESG have to be seen as “package”
 - “Sensible” interpretation of extreme scenarios
 - Ability to price options & guarantees by ESG must be sufficient for the options & guarantees intrinsic to the liabilities
 - A bad valuation model cannot be saved by a good ESG
 - Dependency on particular ESG should be minimized

Relevant criteria:

Confirmation by Appointed Actuary

FINMAs attempt at testing the adequacy of the interest rate model

- Test 1: What are the relevant market prices to calibrate to?
 - Using a simplified replicating portfolio approach: asset universe restricted to swaps and (liquid) swaptions
 - “Weights” assigned to swaptions indication for “relevance”
- Challenges:
 - Big fitting error expected
 - Results dependent on scenario set used
 - Solution might not be very robust; high offsetting positions
 - Big effort
- However,
 - RP not used for (re-) valuations, so quality of fit not so much of an issue
 - Should be run with IR that can fit IR-vol surface well
 - Interested in an indication of region to calibrate to
 - Particularly suitable for companies already using an RP-approach

FINMAs attempt at testing the adequacy of the interest rate model

- Test 2: What impact has a change of the interest rate model?
- Challenges:
 - Change of IR-model not without implications on asset model
 - Impact might not be attributable to a specific characteristic
- However,
 - Use for both valuations simplified asset model (e.g. following Brownian motion)
 - Change IR-model only gradually
 - 1-factor to 2-factor, keeping distribution
 - normal vs. lognormal, keeping # of factors
 - consistent calibration approach, using results of test 1

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